

ABOUT ONE ISSUE OF DELAYED DIFFERENTIAL PLAY

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Abstract

The article explores the method of directional chasing to solve conflict state problems characterized by a neutral-type differential equation with a delay argument, as well as the method of decisive functions in solving the problem of chasing, the apparatus of differential and differential-differential equations, the mathematical theory of optimal processes, theories of differential games, the theory of multivariate reflections.

Us motion vector z_1, \dots, z_k s with that identify, n -dimensional E^n euclid in space

$$z'_i = C_i z_i + u_i + v, \quad 1 \leq i \leq k, \quad (1.1)$$

linear differential equations given are. This land, C_i - $n \times n$ -dimensional constant in matrix, $u_i \in U_i, v \in V, U_1, \dots, U_k, V$ - the orientation of a convex compact package.

Also to us, M_1, \dots, M_k - closed, convex, the orientation of the E^n euclid space to the appropriate packages given are. Variables of a multiple that it is the condition representing (1.1) differential in the game chases group $P = \{P_1, \dots, P_k\}$ and prohibition realistically to the player (which escape) E are. In the game chases the group P , the management of vector $u = \{u_1, \dots, u_k\}$'s instructions according and any z_i vector in the corresponding basis on M_i ($1 \leq j \leq k$) the terminal in the package come down to the effort that will make. The player (which escape) E for his v guidance in M_i ($1 \leq j \leq k$) the collection to come down and not move does.

(1.1) of the game 's starting point $z^0 = (z_1^0, \dots, z_k^0)$ is, to him suitable time $t(z^0)$ that is a sign let. You any of how the piece of continuous management $v(\cdot)$ to suited so that you manage to $u(\cdot) = (u_1(\cdot), \dots, u_k(\cdot))$ choose, you can, fit without, $j(1 \leq j \leq k)$ $z_j(t_1) \in M_j, t_1 \leq t(z^0)$ it is.

Us closed and convex, the orientation of which is M the package given is if its base function

$$W_M(\psi) = \sup_{x \in M} \langle \psi, x \rangle$$

is and a closed convex orientation conus

$$K_M = \{\psi : W_M(\psi) < +\infty\}$$

if, this $W_M(\psi)$ function K_M at continuous is. The last equality M_i is a compact package, the case is made in.

Us $N_i(q)$, ($1 \leq i \leq k$) – continuous convex value and compact package, as well as $q \in Q$ the orientation of a convex and compact package is given, which is ($N_i(q) \in E^n$).

Now

$$\lambda_i(q) = \min_{\|\psi_i\|=1} [W_{N_i(q)}(\psi_i) + W_{M_i}(-\psi_i)] \quad (1.2)$$

the expression we do not look.

3.1-lemma.

$$\bigcup_{i=1}^k (N_i(q) \cap M_i) = \emptyset \text{ is,}$$

when $\min_{q \in Q} \max_{1 \leq i \leq k} \lambda_i(q) < 0$, if, thus, $q \in Q$.

Proof. Any $q_0 \in Q$ for $\bigcup_{i=1}^k (N_i(q_0) \cap M_i) = \emptyset$ that show needed to be.

Then volunteer $i=1,2,\dots,k$ $N_i(q_0) \cap M_i = \emptyset$. the last of our equal, just $\max_{1 \leq i \leq k} \lambda_i(q_0) < 0$ and fit basis $\min_{q \in Q} \max_{1 \leq i \leq k} \lambda_i(q) < 0$ when it is appropriate is.

Contrary $q_1 \in Q$ to while $\min_{q \in Q} \max_{1 \leq i \leq k} \lambda_i(q) = \max_{1 \leq i \leq k} \lambda_i(q_1)$. theorem from use each a $i-s$ for $N_i(q_1) \cap M_i = \emptyset$ also,

$$\bigcup_{i=1}^k (N_i(q) \cap M_i) = \emptyset$$

the fact that it came out.

Given z_0 the initial cases of character, $u(\cdot)$ and $v(\cdot)$ controls (1.1) equation Cauchy to the formula according to the following appearance comes in.

$$z(t) = z(z^0, t, u(\cdot), v(\cdot)) = \Phi(t)z^0 + \int_0^t \Phi(t-\tau)[u(\tau) + v(\tau)]d\tau \quad (1.3)$$

this earth $\Phi(t)$ – matrix in $\dot{\Phi}(t) = C\Phi(t)$, $\Phi(0) = I$ terms you will build. This I – unit in matrix.

The following yield will

$$A = \left\{ \alpha = (\alpha_1, \dots, \alpha_k) : \alpha_i \geq 0, \sum_{i=1}^k \alpha_i = 1, \alpha_i \in E^1 \right\} \quad (1.4)$$

$$\Psi = \left\{ \psi = (\psi_1, \dots, \psi_k) : \|\psi_i\| = 1, \psi_i \in E^n \right\} \quad (1.5)$$

$$W(z, t, \alpha, \psi) = \sum_{i=1}^k \alpha_i \left\langle \Phi_i^*(t) \psi_i, z_i \right\rangle + \sum_{i=1}^k \alpha_i \int_0^t \max_{u_i \in U_i} \left\langle \Phi_i^*(\tau) \psi_i, u_i \right\rangle d\tau + \int_0^t \min_{v \in V} \left\langle \sum_{i=1}^k \alpha_i \Phi_i^*(\tau) \psi_i, v \right\rangle d\tau \quad (1.6)$$

$$\mu(z, t, \alpha, \psi) = W(z, t, \alpha, \psi) + \sum_{i=1}^k \alpha_i W_{M_i}(-\psi_i) \quad (1.7)$$

$$\lambda(z, t) = \max_{\alpha \in A} \min_{\psi \in \Psi} \mu(z, t, \alpha, \psi) \quad (1.8)$$

You in advance agreed, unless, in the game, the current controls $v(\cdot), u_1(\cdot), \dots, u_k(\cdot)$ if, this time, $0 \leq \tau \leq t$ is, $v(\tau), u_i(\tau) \in U_i, (1 \leq i \leq k)$ - dimensional functions, we understand.

Given $v(\cdot)$ the current administration, optional $i, 1 \leq i \leq k$ s for the following, don't look at

$$N_i(z_i, t, v(\cdot)) = \{z_i(t) : z_i(t) = \Phi_i(t)z_i + \int_0^t \Phi_i(t-\tau)u_i(\tau)d\tau + \int_0^t \Phi_i(t-\tau)v(\tau)d\tau,$$

$$u_i(\tau) \in U_i, 0 \leq \tau \leq t\},$$

$$W_{N_i(z_i, t, v(\cdot))}(\psi_i) = \left\langle \Phi_i^*(t) \psi_i, z_i \right\rangle + \int_0^t \max_{u_i \in U_i} \left\langle \Phi_i^*(\tau) \psi_i, u_i \right\rangle d\tau + \int_0^t \left\langle \Phi_i^*(\tau) \psi_i, v \right\rangle d\tau,$$

$$\lambda_i(z_i, t) = \min_{\|\psi_i\|=1} \left[W_i(z_i, t, \psi_i) + W_{M_i}(-\psi_i) \right].$$

Now form those who make the above function with we are bound.

3.1-teorama. *The following relationship fitting*

$$\lambda(z_i, t) \leq \min_{v(\cdot)} \max_{1 \leq i \leq k} \lambda_i(z_i, t, v(\cdot)) \quad (1.9)$$

$$\lambda(z, t) \leq \max_{1 \leq i \leq k} \lambda_i(z_i, t) \quad (1.10)$$

Proof. Every how $v(\cdot)$ the current administration for

$$\max_{\alpha \in A} \left[\sum_{i=1}^k \alpha_i \lambda_i(z_i, t, v(\cdot)) \right] \geq \max_{\alpha \in A} \min_{\psi \in \Psi} \left[\sum_{i=1}^k \alpha_i \left\langle \Phi_i^*(t) \psi_i, z_i \right\rangle + \right. \quad (1.11)$$

$$\left. + \sum_{i=1}^k \alpha_i \int_0^t \max_{u_i \in U_i} \left\langle \Phi_i^*(\tau) \psi_i, u_i \right\rangle d\tau + \min_{v(\cdot)} \int_0^t \left\langle \sum_{i=1}^k \alpha_i \Phi_i^*(\tau) \psi_i, v(\tau) \right\rangle d\tau \right]$$

To us $\varepsilon_1, \dots, \varepsilon_k$ - is given is

$$\max_{\alpha \in A} \left[\sum_{i=1}^k \alpha_i \varepsilon_i \right] = \max_{1 \leq i \leq k} \varepsilon_i \quad (1.12)$$

the formula according to the following results possible you will be

$$\max_{\alpha \in A} \left[\sum_{i=1}^k \alpha_i \lambda_i(z_i, t, \nu(\cdot)) \right] = \max_{1 \leq i \leq k} \lambda_i(z_i, t, \nu(\cdot)) \quad (1.13)$$

That's in addition to the following relation on from on bring a can

$$\min_{\nu(\cdot)} \int_0^t \left\langle \sum_{i=1}^k \alpha_i \Phi_i^*(t-\tau) \psi_i, \nu(\tau) \right\rangle d\tau = \int_0^t \min_{\nu \in V} \left\langle \sum_{i=1}^k \alpha_i \Phi_i^*(\tau) \psi_i, \nu \right\rangle d\tau \quad (1.14)$$

Therefore, (1.1) in the expression, is (1.13) and (1.14) relationship considering beneficially (1.9) the relationship is reasonable that show easy.

(1.10) the relationship we will prove

$$\min_{\nu \in V} \left[\left\langle \sum_{i=1}^k \alpha_i \Phi_i^*(\tau) \psi_i, \nu \right\rangle \right] \geq \sum_{i=1}^k \alpha_i \min_{\nu \in V} \langle \Phi_i^*(\tau) \psi_i, \nu \rangle$$

also

$$\mu(z, t, \alpha, \psi) \geq \sum_{i=1}^k \alpha_i [W_i(z_i, t, \psi_i) + W_{M_i}(-\psi_i)].$$

So make

$$\lambda(z, t) \geq \max_{\alpha \in A} \min_{\psi \in \Psi} \sum_{i=1}^k \alpha_i [W_i(z_i, t, \psi_i) + W_{M_i}(-\psi_i)],$$

the relationship is made. (1.12) and the relations (1.10) of the relationship private is free.

The game finish time and his analyst will feature.

To us, the initial state is a $z^0 = (z_1^0, \dots, z_k^0)$ form fixed

$$I(z^0) = \{i : z_i^0 M_i, 1 \leq i \leq k\}$$

the package given is.

3.1-lemma to according say that $I(z^0) = \emptyset$ is, when $\lambda(z^0, 0) < 0$ it is. You $I(z^0) \neq \emptyset$ if, so $T(z)$ the function we determine it z^0 at $T(z^0) = 0$ are. You $I(z^0) = \emptyset$ have $T(z^0)$ as the equation of the first positive root $\lambda(z^0, t) = 0$ as we can. The remaining case $T(z^0) = +\infty$.

$T(z)$ the function of the meaning more accurate understanding for following lemma in the mix come.

3.2 - lemma. $T(z^0) < +\infty$ is any how $\nu(\cdot)$ current management $j(1 \leq i \leq k)$ procedure on being found, for him to fit, which comes to the current administration $u_i(\cdot)$ by a determined, all $z_j(z_j^0, T(z^0), u_j(\cdot), \nu(\cdot)) \in M_j$ that is.

Proof. You prove not only of the game z_0 the initial state to see out enough is, $I(z^0) = \emptyset$ that to show difficult it is.

Identified $T(z)$ function for $\lambda(z^0, T(z^0)) = 0$. That (1.9) the relationship is as follows: write you can

$$\min_{\nu(\cdot)} \max_{1 \leq i \leq k} \lambda_i(z_i^0, T(z^0), \nu(\cdot)) \geq 0$$

now the 1.1 - to lemma according optional $\nu(\cdot)$ current management for

$$\bigcup_{i=1}^k [N_i(z_i^0, T(z^0), \nu(\cdot)) \cap M_i] \neq \emptyset$$

expression of the form we make. This last expression from the lemma confirmation come out.

Us $\nu(z, t, \alpha) = \min_{\psi \in \Psi} \mu(z, t, \alpha, \psi)$ function and

$$A(z, t) = \{\alpha \in A : \nu(z, t, \alpha) = \lambda(z, t)\}, \quad \Psi(z, t, \alpha, \psi) = \nu(z, t, \alpha)$$

to package given.

$A(z, t)$ to package to relevant $\{z, t\}$'s α to citizens of the continuous image of $\Psi(z, t, \alpha)$. $\Psi(z, t, \alpha)$ the image $\alpha \in A(z, t)$ is A a package of each a point to be made. Again $e' = (e, \square)$ given is, thus, $e = (e_1, \dots, e_k)$, $e_i - n -$ dimensional vector, \square - of any number.

The following write you can

$$\frac{\partial \lambda}{\partial e} = \sup_{\alpha \in A(z, t)} \min_{\psi \in \Psi(z, t, \alpha)} [\langle \partial_z \mu(z, t, \alpha, \psi), e \rangle + \square \partial_t \mu(z, t, \alpha, \psi)] \quad (1.15)$$

this here $\partial_z \mu - \mu$'s z on gradient function, $\partial_t \mu - t$ on to get derivative. Also $A(z, t)$ from taken and $\Psi(z, t, \alpha)$ the collection $\{z, t\}$ point fixed $\alpha \in A(z, t)$ at the point $\Psi(z, t, \alpha)$ the function from above semi - continuous is.

(1.6) and (1.7) formula use

$$\partial_z \mu(z, t, \alpha, \psi) = (\alpha_1 \Phi_1^*(t) \psi_1, \dots, \alpha_k \Phi_k^*(t) \psi_k) \quad (1.16)$$

$$\partial_z \mu(z, t, \alpha, \psi) = \sum_{i=1}^k \alpha_i \langle \Phi_i^*(t) \psi_i, C_i z_i \rangle + \quad (1.17)$$

$$+ \sum_{i=1}^k \alpha_i \max_{u_i \in U_i} \langle \Phi_i^*(t) \psi_i, u_i \rangle + \min_{\nu \in V} \langle \sum_{i=1}^k \alpha_i \Phi_i(t) \psi_i, \nu \rangle$$

If (1.12) to the expression of $e' = \{0, 1\}$ and $e' = \{0, -1\}$ to have put

$$\left(\frac{\partial \lambda}{\partial t}\right)^+ = \sup_{\alpha \in A(z,t)} \min_{\psi \in \Psi(z,t,\alpha)} \partial_t \mu(z,t,\alpha,\psi),$$

$$\left(\frac{\partial \lambda}{\partial t}\right)^- = - \inf_{\alpha \in A(z,t)} \max_{\psi \in \Psi(z,t,\alpha)} \partial_t \mu(z,t,\alpha,\psi),$$

that is, it $\left(\frac{\partial \lambda}{\partial t}\right)^+$ and $\left(\frac{\partial \lambda}{\partial t}\right)^-$ the expression $\lambda(z,t)$ from t by taken the left and right surge whom finds doing so means.

Comments. Following

a) $0 < T(z) < \infty;$

b) $\inf_{\alpha \in A(z,T(z))} \max_{\psi \in \Psi(z,T(z),\alpha)} \partial_t \mu(z,T(z),\alpha,\psi) > 0;$

conditions is carried out, $z = (z_1, \dots, z_k)$ to the point regular point is called.

You Ω - regular - point package that beneficially, his close $\bar{\Omega}$ with and its border $\omega = \bar{\Omega} / \Omega$ with we will write.

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